High Resolution Simulation of Full Aircraft Control at Flight Reynolds Numbers (Challenge C2D)

Scott A. Morton	David R. McDaniel	Keith Bergeron	Stefan Goertz
USAF Seek Eagle Office	USAF Academy	USAF Academy	USAF Academy
Scott.Morton@eglin.af.mil	David.McDaniel.ctr@usafa.af.mil	Keith.Bergeron@usafa.af.mil	Stefan.Gortz@usafa.af.mil
Russell M. Cummings	James R. Forsythe	Jurgen Seidel	Kyle D. Squires
USAF Academy	Cobalt Solutions, LLC	USAF Academy	Arizona State University
Russ.Cummings@usafa.af.mil	Forsythe@cobaltcfd.com	Jurgen.Seidel.ctr.de@usafa.af.mil	Squires@asu.edu

Introduction

This paper documents progress in the second year of a three year challenge project to develop a computational method for accurately determining static and dynamic stability and control of fighter and transport aircraft. There are three phases to the research plan which roughly align with FY06, FY07, and FY08. In the first year, forced motion time-accurate simulations of rigid body aircraft grids are performed to determine static and dynamic stability characteristics, as well as, six degree-of-freedom motions (6DOF). In the second year, "computational maneuvers" are developed to efficiently build a stability and control reduced order model and moving control surfaces are implemented. Also, prescribed motions of flight test maneuvers are computed to determine the ability of the "computational maneuvers" to predict aircraft response of actual flight test maneuvers such as wind-up turns (WUTs), pitch-over pull-ups (POPUs), and rudder doublets (RDs). In the third year, inner loop control laws are added to the simulation to allow aircraft pilot inputs to the simulations and 6DOF motions are tracked. The pilot inputs will be those that result in WUTs, POPUs, and RDs. This third year is essentially a "virtual flight test" and represents a large step forward in vehicle modeling and simulation. All simulations incorporate advances in full aircraft simulations at flight Reynolds numbers experiencing massively separated flows resulting from the previous challenge (C92).

Objective

The C2D Challenge project objective is to develop a methodology for efficient and accurate screening for nonlinear aerodynamic phenomena such as spin, tumble, lateral instabilities, limit cycle oscillations, and tail buffet of full aircraft. The first goal is to efficiently compute DoD fighter and transport aircraft stability and control data across the flight envelope. The second goal is to compute **dynamic** stability and control/control effectiveness data that is extremely difficult to obtain in the wind tunnel. The third goal is to develop **maneuvers** that can discover undesirable flight control/flying qualities attributes prior to flight test.

Methodology

A second year step towards achieving the above objectives is to predict force and moment coefficient data for the F-16C to determine static and dynamic stability and control characteristics. Static and dynamic simulations of the F-16C are computed using *Cobalt* and the Detached-Eddy Simulation (DES) turbulence treatment on adaptively refined meshes. Maneuvers of the F-16C such as pitch, yaw and pitch-yaw chirps are computed using the rigid body motion option in Cobalt. System identification is then used to develop a reduced order model of the F-16C. Comparisons are then made between CFD simulations of flight test maneuvers such as wind up turns, rudder doublets, and pitch doublets and the derived model for verification. The model can then be used for any additional maneuvers within the range of applicability of the reduced order model.

Significance to DoD

Practically every fighter program since 1960 has had costly nonlinear aerodynamic or fluid-structure interaction issues discovered in flight test. A method of computing solutions across the envelope will allow computational simulations to impact the design cycle as opposed to simply diagnosing an existing problem, saving significant acquisition costs.



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Russ.Cummings@usafa.af.mil	Forsythe@cobaltcfd.com	Jurgen.Seidel.ctr.de@usafa.af.mil	Squires@asu.edu

Abstract

This paper documents interim results of a three year project to develop a computational method for accurately determining static and dynamic stability and control characteristics of fighter and transport aircraft with various store configurations, as well as the aircraft response to pilot input. In this second year of the project computational data is gathered for a rigid F-16C with no control surface movement in forced motion that approximates flight test maneuvers. "Computational maneuvers" designed to efficiently gather three axes of motion data to build a comprehensive reduced order model are also developed. The data is then post-processed to determine the resulting static and dynamic stability characteristics. The main benefits of this effort are: 1) early discovery of complex aerodynamic phenomena that are typically only present in dynamic flight maneuvers and therefore not discovered until flight test, and 2) rapid generation of an accurate aerodynamic database to support aircraft and weapon certification by reducing required flight test hours and complementing current stability and control testing.

1. Introduction

PRACTICALLY every fighter program since 1960 has had costly nonlinear aerodynamic or fluid-structure interaction issues discovered in flight test. The main reason for these "failures" is that the predictive methods used were not able to reveal the onset and nature of the problems early in the design phase. To keep the budget overshoot under control, fixes tend to be *ad hoc* and are applied without a sound basis of fundamental understanding of the physics concerned. Unfortunately, in future aircraft designs, the problems will only become more complex as thrust vectoring, active aeroelastic structures, and other related technologies are implemented for stability and control augmentation. Unmanned combat vehicles will operate in flight regimes where highly unsteady, nonlinear, and separated flow characteristics dominate since there are no man-rating requirements [1]. In order to decrease the costs incurred by extensive flight-tests and the post-design phase modifications, it would be helpful to have a tool which enables aircraft designers to analyze and evaluate the non-linear flight-dynamic behavior of the aircraft and/or associated armament, in the form of stability and control (S&C) characteristics, early in the design phase.

The present paper provides an update on the first-year effort to develop a high-fidelity simulation environment that will bring together aerodynamics, aeroelasticity and flight mechanics into a time accurate simulation tool. The benefits from such a tool to the areas of aircraft stability and control, flight simulation, and aircraft and weapon certification could potentially result in savings reaching into the billions of dollars [2]. The paper begins with a review of previous research in the field, followed by the objectives of this research. Next, the status of the tools being developed to support this effort is discussed. Finally, some preliminary results are presented.

2. Numerical Method

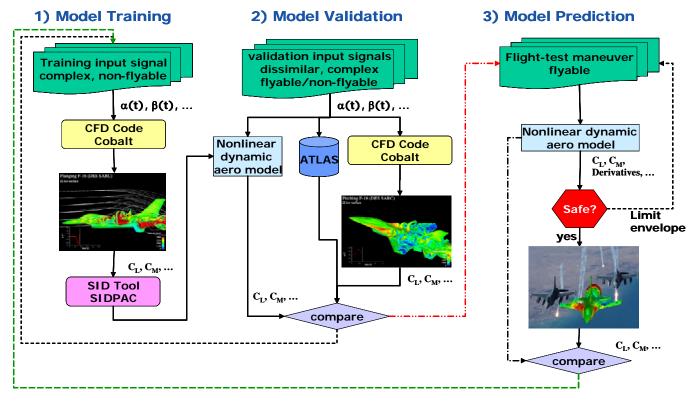


Figure 1: Stability and Control Model Build Process

This section presents the method of building an aircraft model suitable for determining the stability and control characteristics of fighter aircraft in the entire aircraft envelope. The first step in the method is to build a geometric representation of the complete aircraft of interest (including stores, control surfaces, inner loop control laws, aeroelastic effects, etc.). Next, simulations are performed of maneuvers designed to excite the relevant flow physics that will be encountered during actual missions in all three axes, roll, pitch, and yaw. These simulations are termed "computational maneuvers," since they may be unreasonable to fly due to actual aircraft or pilot limits. Next, a mathematical model is built of the aircraft response using system identification. Then, the model is tested by comparing CFD simulations against model predictions of simulations expected to be encountered in flight. Finally, predictions of all flight test points are made using the model before flight tests are conducted to determine the expected behavior of the actual aircraft. Figure 1 depicts this process graphically. The following sub-sections describe the individual elements of the flow solver and system identification method necessary for the process.

Flow Solver

Computations are performed using the commercial flow solver *Cobalt*. *Cobalt* is a cell-centered, finite volume CFD code. It solves the unsteady, three-dimensional, compressible Reynolds Averaged Navier-Stokes (RANS) equations on hybrid unstructured grids. Its foundation is based on Godunov's first-order accurate, exact Riemann solver. Second-order spatial accuracy is obtained through a Least-Squares Reconstruction. A Newton subiteration method is used in the solution of the system of equations to improve time accuracy of the point-implicit method. Strang *et al* [3] validated the numerical method on a number of problems, including the Spalart-Allmaras (SA) model, which forms the core for the Detached Eddy Simulation (DES) model available in *Cobalt*. Tomaro *et al* [4] converted the code from explicit to implicit, enabling CFL numbers as high as 10⁶. Grismer *et al* [5]

parallelized the code, yielding linear speed-up on as many as 2,800 processors. The parallel METIS (PARMETIS) domain decomposition library of Karypis *et al* [6] is also incorporated into *Cobalt*. New capabilities include rigid-body and 6 DOF motion, equilibrium air physics, Dynamic DES [7] and overset grids in release *Cobalt V4.0*. A coupled aeroelastic simulation capability is also being developed.

System Identification Analysis (SIDPAC)

System identification (SID) is the process of constructing a mathematical model from input and output data for a system under testing, and characterizing the system uncertainties and measurement noises [8]. The mathematical model structure can take various forms depending upon the intended use. SID is usually applied to wind-tunnel and flight-test data to obtain accurate and comprehensive mathematical models of aircraft aerodynamics, for aircraft flight simulation, control system design and evaluation, and dynamic analysis. A very comprehensive review of SID applied to aircraft can be found in Morelli and Klein [9,10] and Jategaonkar [11,12].

Aircraft system identification can be used in cooperative approaches with CFD, to take advantage of the strength of both approaches or having one approach fill in the gaps where the other cannot be used effectively [9]. The wide range of SID tools that have been developed for aircraft system identification can easily be used to analyze CFD data computed for aircraft in prescribed motion. Here we follow the global nonlinear parameter modeling technique proposed by Morelli [13] to describe the functional dependence between the motion and the computed aerodynamic response in terms of force and moment coefficients. The goal is to find a model which has adequate complexity to capture the nonlinearities while keeping the number of terms in the model low. The latter requirement improves the ability to identify model parameters, resulting in a more accurate model with good predictive capabilities. The modeling effort is global because the independent variables (α , $\dot{\alpha}$, β , etc.) are varied over a large range. Globally valid analytical models and their associated smooth gradients are useful for optimization, robust nonlinear control design and global nonlinear stability and control analysis.

3. F-16 Results

To date, a full-scale F-16 undergoing the following prescribed motions has been simulated: "computational maneuvers"-- continuous α sweep, sinusoidal pitching, coning motion, oscillatory coning, configuration plunge pulse, plunge chirp, pitch chirp, Schroeder plunge, yaw chirp, composite pitch-yaw chirp, and flight test maneuvers -- pitch doublet, and wind up turn. These motions represent both computational maneuvers and flight test maneuvers for stability and control testing and were defined using an interactive GUI. Variations in Mach number from subsonic (M = 0.3 – 0.6), transonic (M = 0.85 – 0.95) to supersonic (M = 1.2) were computed at a Reynolds number (Re) of approximately 15 million. Many of the maneuvers have been covered in detail in previous papers (References [14], [15], [16], [17], [18], [19]) but the current paper will focus on various chirp signals and the flight test maneuvers not previously presented.

The grid used here for symmetric maneuvers is a half-span, full-scale model of the F-16 and non-symmetric maneuvers use the same grid mirrored about the symmetry plane. The model includes the forebody bump, diverter, and ventral fin. The engine duct is modeled and meshed up to the engine face. The wing-tip missile and corresponding attachment hardware are not modeled, however, nor is the nose boom. The 3D hybrid grid was generated using the NASA Langley grid generation packages GRIDTOOL [20] and VGRIDNS [21], as well as the *Cobalt L.L.C.* grid management utility BLACKSMITH [22]. The surface grid comprises 167,382 elements and off the surface there are eight prismatic layers. The height of the first prismatic layer corresponds to an average wall y^+ value of less than four. In total there are 3.2 million cells with cells concentrated in the strake vortex. A full span grid with 6.4 million cells was created by mirroring cells across the symmetry plane for maneuvers that require a full span grid (e.g. coning, oscillatory coning). The boundary conditions are symmetry, adiabatic solid wall for the surface of the aircraft and the engine duct, and modified Riemann invariants for the far-field

boundaries. A source boundary condition based on Riemann invariants is used to create an inflow condition at the engine exhaust. A sink boundary condition is used at the engine face to model the corrected engine mass flow.

The unsteady maneuvers were simulated using the DES, Spalart-Allmaras one-equation hybrid Reynolds-averaged/large eddy simulation turbulence model with the streamline curvature and rotation correction (DESSARC) to predict the effects of fine scale turbulence. Fully turbulent flow was assumed. The outer (physical) time step was set to Δt =0.0004s, corresponding to a non-dimensional time step (in terms of chord and freestream velocity) of Δt *=0.01. The number of Newton sub-iterations was set to 5. The unsteady numerical simulations were initialized by steady-state solutions computed with the Spalart-Allmaras RANS model with the streamline curvature and rotation correction (SARC).

The majority of the static validation computations were run on 64 to 128 processors on "Iceberg", an 800-processor IBM Power4 system operated by the Arctic Region Supercomputing Center (ARSC). All of the larger computations involving grid motion were run on 128-512 processors on either "Babbage", a 3072-processor IBM Power5+ (1.9GHz) distributed-memory system operated by the Naval Oceanographic Office (NAVO) or "Jaws", a 5120-processor Dell PowerEdge 1955 blade server cluster (3.0GHz, dual core) with Infiniband interconnect operated by the Maui High Performance Computing Center (MHPCC).

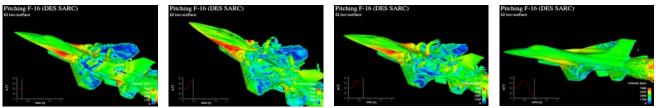


Figure 2: DES of F-16 in sinusoidal pitching motion of the initial stages of the Pitch Chirp; instantaneous vorticity isosurface colored by magnitude of velocity.

Chirp Grid Motion Inputs

Based on a cursory evaluation of a number of different motion types, it was determined that a simple chirp input applied to either a plunge or a rotational grid motion led to reduced order models with the best overall dynamic predictive capability. This is most likely due to the fact that the broad range of frequencies in the chirp signal excites the aerodynamic system over a large range of angle of attack, angle of sideslip, pitch rate, etc. Figure 2 above depicts typical flowfield snapshots during a pitch chirp maneuver. The relationship used to create these chirp signals is the same as that used in the "chirp" function in MATLAB[®] and is given in Equation 1.

$$s(t) = \cos\left(2\pi\left(\frac{\beta}{\lambda + 1}t^{\lambda + 1} + f_1t + \frac{\phi}{360}\right)\right) \text{ where } \beta = \left(\frac{f_2 - f_1}{t_2^{\lambda}}\right)$$
 (1)

The parameters f_1 and f_2 denote the low and high limits of the chirp frequency bandwidth, respectively. The parameter t_2 is the time length of the chirp signal, and the parameter ϕ provides the ability to apply a phase shift to the signal as needed to help control whether or not the signal is biased relative to the starting amplitude. For a given signal length and bandwidth, the parameter, λ , controls the rate at which the signal traverses the requested frequency range. A value of $\lambda = 1.0$ corresponds to a linear change in frequency whereas a value of $\lambda = 2.0$ corresponds to a quadratic change in frequency, and so forth. Figure 3 shows the variation of frequency with time for a number of different values of this parameter.

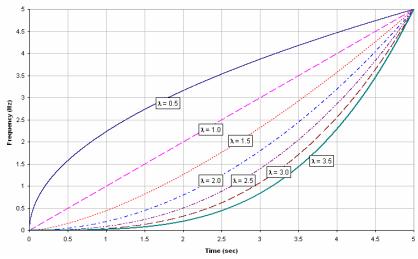


Figure 3: Frequency variation with time for various values of the chirp λ parameter

Figure 4 shows chirp input signals for two different values of λ . The authors are currently investigating the effect of different values of the λ parameter on the ability of models resulting from the various pitch chirp maneuvers to predict both static and dynamic validation data. Past experience has shown that a linear change in frequency in the chirp signal tends to result in poor model predictions of static data. Chirp signals with higher λ values, which effectively dwell at the lower frequencies as seen in Figure 4, will hopefully improve these static predictions.

These various chirp signals have been used to drive both rotational and plunge motion of the CFD grid. While it is a fairly simple task to generate prescribed chirp motions about a single axis, it is more desirable to implement such motions in multiple axes so that the resulting models may be used to predict more complex motion (e.g. yaw-roll maneuvers). It is ultimately desired to be able to excite the aircraft aerodynamics based on motion in all three coordinate axes with a single CFD run. The resulting data could then be used to generate a low-order model for all six force and moment coefficients. Then, these models could be quickly differentiated to provide needed stability derivatives.

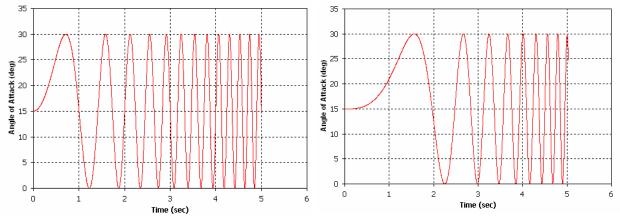


Figure 4: Angle of attack histories for single-axis chirp motions with $\lambda = 1.0$ (left) and $\lambda = 2.0$ (right)

Example Model Fit and Prediction

As discussed above, it is desirable to use multiple-axis motions to generate more capable aerodynamic models versus just single-axis motions which would only be valid for a limited set of maneuvers and test cases. Tools

have been developed to quickly generate multiple axis grid motions by combining multiple chirp signals to drive plunge or rotational motion. It is important for multiple input signals to be as "orthogonal" as possible in order to benefit the multivariate modeling process (i.e. make the resulting polynomial model terms more linearly independent). Therefore, the driver chirp signals for the multi-axis motion are made orthogonal via the λ parameter discussed above. For example, in the case of a two-axis input motion, the λ value for the first driver signal is specified, and the λ value for the second signal is varied until the two signals are orthogonal (defined as a zero inner product).

Figure 5 shows an example of a combined pitch-yaw chirp motion designed to provide angle of attack motion between 0 and 30 degrees and sideslip motion between -15 and +15 degrees. The pitch chirp motion was generated with $\lambda = 1.0$, and the yaw chirp motion was generated with $\lambda = 1.47$ (computed to make the chirp signals orthogonal as discussed above). The left-pane of Figure 5 shows the required grid rotations about the three coordinate axes, and the right-pane shows the resulting angle of attack and sideslip excursions based on the prescribed flow conditions (0.6 Mach, 5000 ft). Note that motion in *all three* coordinate directions is needed since the prescribed yaw motion in this case was about the vertical stability axis versus the vertical body axis. It is clear that this prescribed motion will force the aircraft through a large number of angle of attack/sideslip combinations (and likewise pitch, roll, and yaw rate combinations). This is a much more efficient way to "map" the flight envelope with aerodynamic force and moment coefficients versus running multiple static solutions.

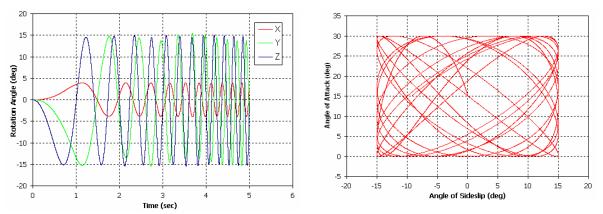


Figure 5: Grid motion (left) and resulting angle of attack/sideslip (right) for combined yaw-pitch chirp maneuver

Figure 6 shows the lift coefficient time history ("training data") plotted against angle of sideslip after implementing the grid motion in Figure 5 for the full-scale F16C at Mach = 0.6 and 5000 ft. Also shown in the figure is the resulting multivariate polynomial fit for lift coefficient using the SIDPAC software with angle of attack, angle of sideslip, roll rate, pitch rate, and yaw rate as model variables. The resulting model equation has the structure shown in Eq 2, where the model terms are listed in order of most influential to least influential. This lift coefficient model results in a goodness of fit value of 99.86%.

$$C_{L}(\alpha, \beta, p, q, r) = C_{1} + C_{2}\alpha + C_{3}q + C_{4}p^{2} + C_{5}\alpha q^{2} + C_{6}\beta pq + C_{7}\beta p + C_{8}\alpha^{2}q + C_{9}r + C_{10}\alpha\beta^{2} + C_{11}\alpha^{3} + C_{12}pr + C_{13}\beta^{2}p + C_{14}\beta^{2}q + C_{15}p + C_{16}\beta^{2}$$
(2)

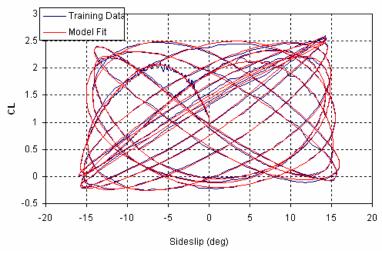


Figure 6: Model fit for combined yaw-pitch chirp maneuver

As mentioned previously, the ultimate desire is to generate efficient yet accurate nonlinear aerodynamic models capable of predicting force and moment coefficients for both static and dynamic aircraft orientations. From these models, stability derivatives may be quickly calculated. Figure 7 shows predictions made with the model in Eq 2 for both static lift curve data (left pane) as well as a pitch-axis oscillatory maneuver (linear chirp). Note that both of these validation data sets were generated from separate CFD runs (versus experimental data), so any errors or discrepancies may be assumed to be due to modeling errors or CFD convergence issues as opposed to vehicle configuration or flight condition differences. It is evident that both predictions match the validation data very well with the exception of the static high angle of attack data (left pane in Figure 7). This is most likely due to the small amount of low-frequency training data available at high angles of attack (due to the prescribed input motion). As mentioned above, chirp motions with different values of λ are being investigated to try and improve these static predictions. Additionally, input motions traversing a larger angle of attack range (including post-stall) are currently being investigated.

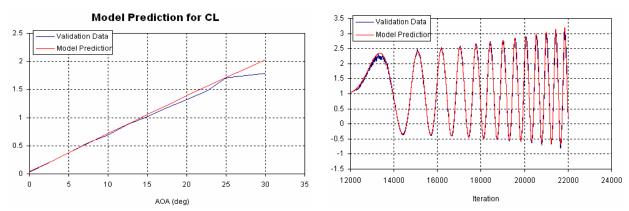


Figure 7: Model prediction of static (left) and dynamic (right) validation data

Flight Test-Derived Maneuvers

The ultimate goal of the modeling process described above is to be able to accurately predict the stability (and eventually control) characteristics of the aircraft during realistic maneuvers. A number of flight test maneuvers such as wind-up turns, yaw-roll doublets, and steady heading sideslips have traditionally been used to evaluate the stability and flying qualities characteristics of an aircraft with a new weapons loading or configuration. Tools have been developed to derive the CFD grid motion needed to aerodynamically model the aircraft during such

maneuvers. The left pane of Figure 8 shows the required grid motion to generate the same aerodynamic parameter histories (body axis rates, angle of attack, angle of sideslip) as an actual F16C flight test maneuver accomplished by personnel at Eglin AFB, Florida. In this case, the flight test maneuver was a 2.5-g wind-up turn. The right-hand pane of Figure 8 shows the measured (raw) angle of attack from the flight test overlaid with the angle of attack computed from the derived grid motion.

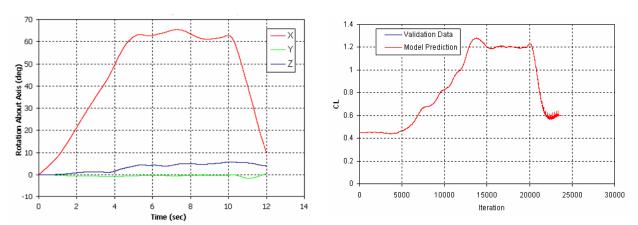


Figure 8: Grid motion (left) and angle of attack time history (right) for wind-up turn flight test maneuver

This maneuver plus a number of additional dynamic validation cases are currently being executed on "jaws" at the Maui High Performance Computing Center. The left pane of Figure 9 shows the required grid motion to emulate an actual pitch doublet flight test maneuver at Mach = 0.6 and 5000 ft (also performed at Eglin AFB, Florida). This grid motion implemented as part of a *Cobalt* flow solution to produce the validation data in the right pane of Figure 9. The polynomial lift coefficient model based on the pitch-yaw chirp maneuver discussed earlier was used to generate the predicted data in the right pane of Figure 9. The validation and prediction data yields a goodness of fit value of 99%. Research into the ability of this and other models to predict various flight test-inspired maneuvers is ongoing.

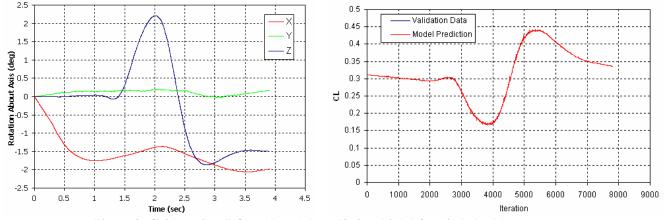


Figure 9: Grid motion (left) and model prediction (right) for pitch doublet maneuver

4. Conclusions and Outlook

The status of a three-year project to develop a computational method for accurately determining static and dynamic stability and control characteristics of fighter and transport aircraft with various weapons configurations as well as the aircraft response to pilot input has been given. Now, just over half-way through the second year of the project, simulation results for the F-16C have been presented. This year marks a transition from computational

simulations of simple motions in a single axis to complex maneuvers in all three axes and simulations of actual flight test maneuvers for verification. The results of the simulations and the proposed analysis process are showing extremely promising results and will result in significantly improved stability and control model building times over the traditional wind tunnel generated database approach, as well as, flexibility when encountering new configurations in the design phase. Comparisons of the results with flight test and wind tunnel data is on-going and will be presented in future papers.

In addition to the maneuver analysis documented in this paper, control surface implementation is occurring in a parallel effort to add control effectiveness characteristics to the analysis method. The first moving control surface simulations will occur in the last quarter of FY07 and will be presented in the final year of the challenge. Additionally, in FY08 the inner loop control laws will be added to the simulation to make the capability equivalent to actual flight test configurations. The method will be used to "shadow" an actual AF SEEK EAGLE certification of a store to show the validity of the method.

FY07 Related References and Awards

There were four conference papers [15,17,18,19], one Maui Applications Brief [16], and two national awards [15,19] associated with the Stability and Control project in FY07:

Reference [15], Winner - ITEA National Symposium Best Poster Paper

Reference [19], Winner - AIAA Air Force Test and Evaluation Days Best Paper

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